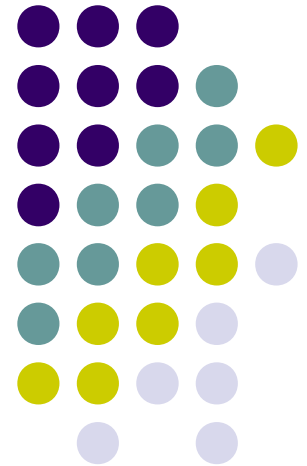


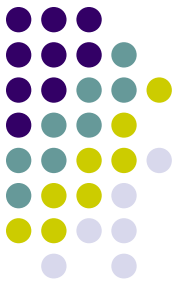
Techniques for the Parametrization of DES Templates

Lenko Grigorov and Karen Rudie

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Queen's University
2010



Motivation (templates)



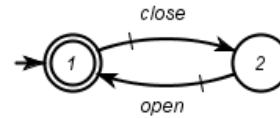
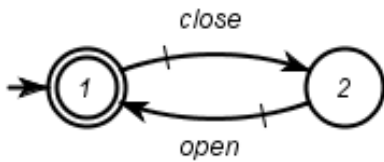
Press 1



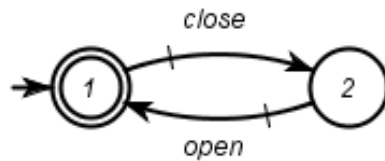
Press 3

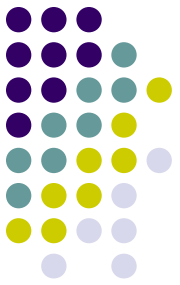


Press 2



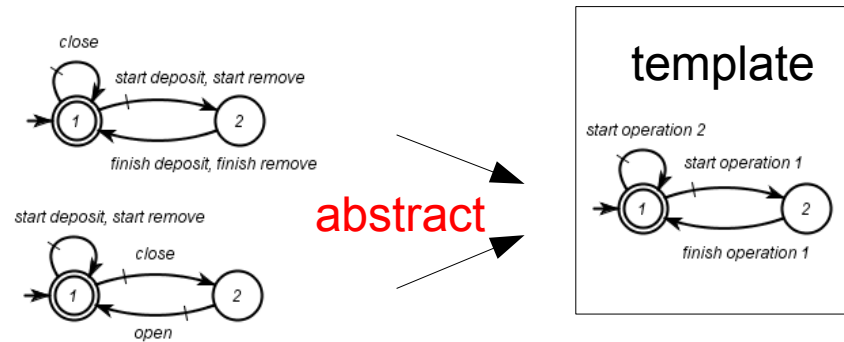
...



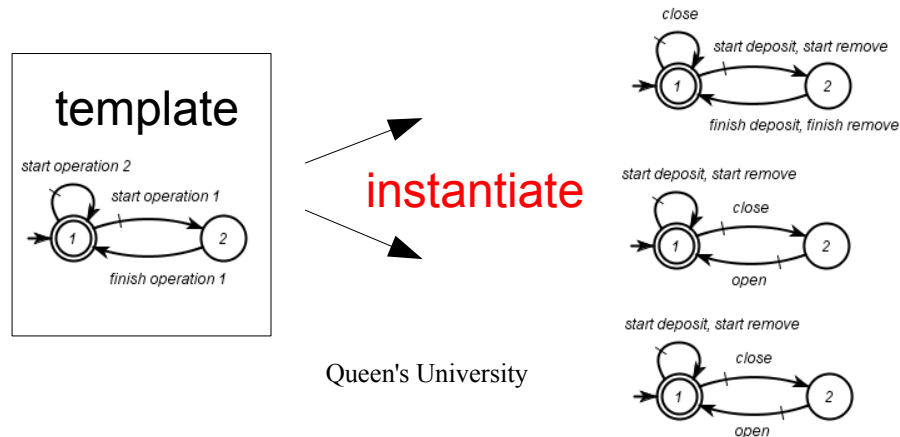


What are templates

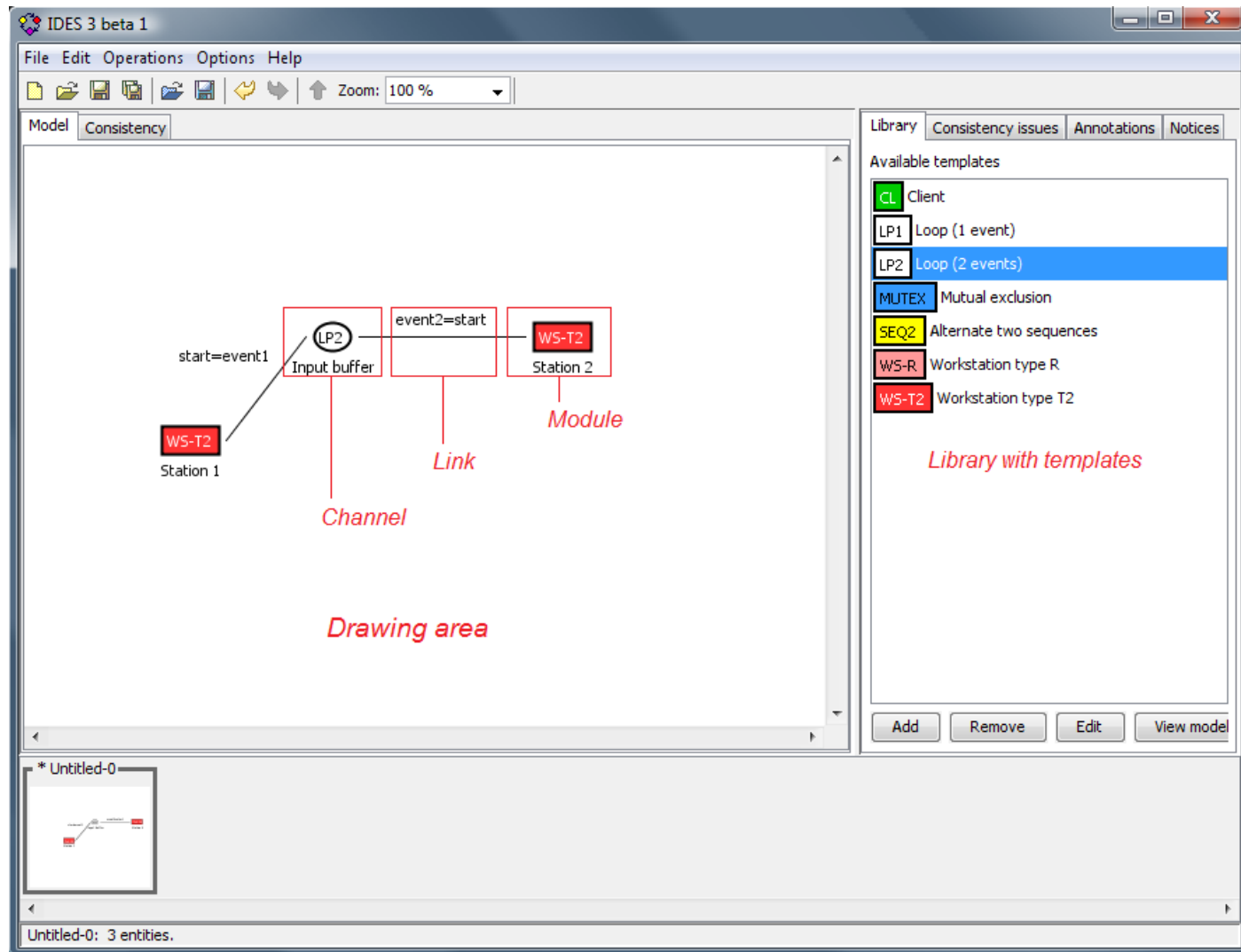
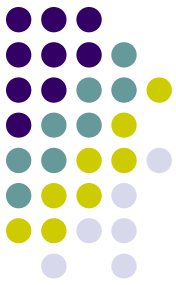
- DES models which
 - Abstract common behavior

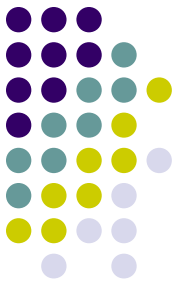


- Can be instantiated to create new models



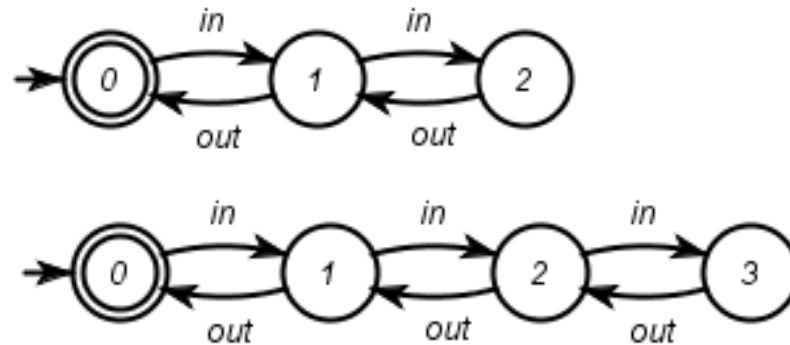
Template design environment





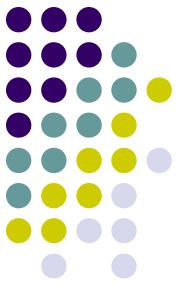
Motivation (parametrization)

- A template is a fixed model
 - So... a separate template for each buffer capacity?



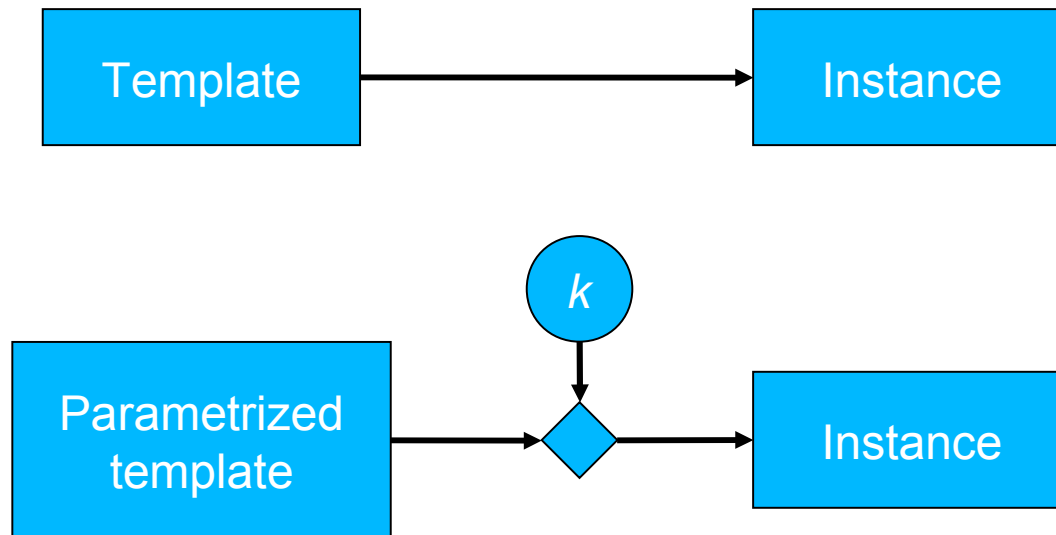
etc...

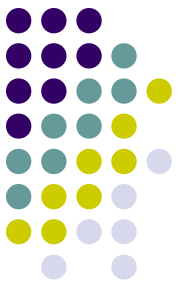
- Why not just parametrize?



Goal

Develop parametrization techniques to produce model instances from templates, given a parameter





Two techniques

- **Parametrization using variables**
 - For example, use Extended Finite Automata from Sköldstam, M., Åkesson, K., and Fabian, M. (2007). Modeling of discrete event systems using finite automata with variables. In *Proceedings of the 46th IEEE Conference on Decision and Control*, 3387–3392. New Orleans, LA, USA
- **Compositional parametrization**
 - Similar in spirit to Bherer, H., Desharnais, J., and St-Denis, R. (2009). Control of parameterized discrete event systems. *Discrete Event Dynamic Systems: Theory and Applications*, 19(2), 213–265

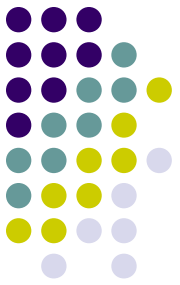
Parametrization using variables



- Can be used to parametrize the *occurrences* of events
- The finite automaton is extended with
 - (finite-interval) variables
 - update functions
 - transition guards
- An algorithm exists to convert extended finite automata to “flat” finite automata

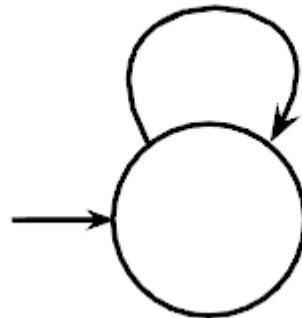
Example 1

Buffer



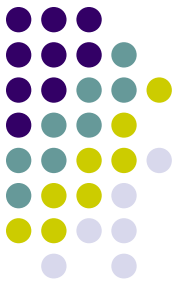
- Parameter k
- Variable n from $[0, k]$
 - initial value $n=0$
 - accepting value $n=0$

$\mathbf{in} \wedge n < k / n := n + 1, \mathbf{out} \wedge n > 0 / n := n - 1$



Example 1

Buffer

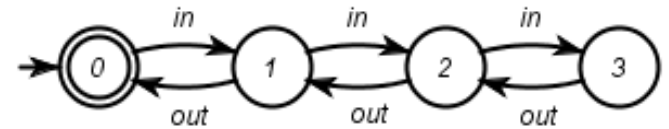
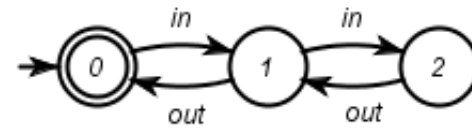


Parameter k

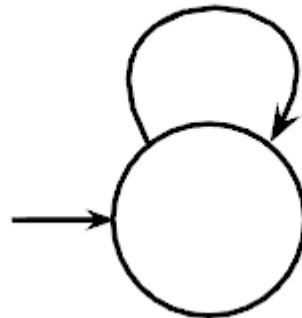
Variable n from $[0, k]$

initial value $n=0$

accepting value $n=0$

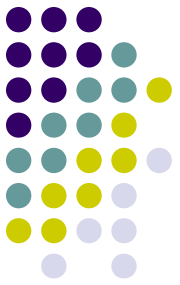


$$\text{in} \wedge n < k / n := n + 1, \text{out} \wedge n > 0 / n := n - 1$$



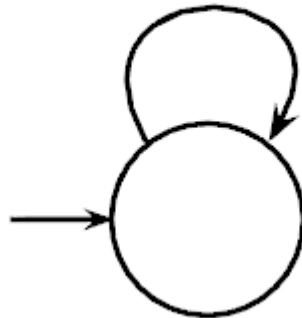
Example 2

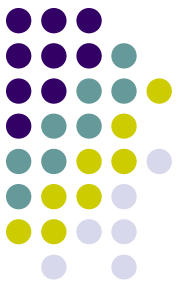
Event occurs k times



- Parameter k
- Variable n from $[0, k]$
 - initial value $n=0$
 - accepting value $n=k$

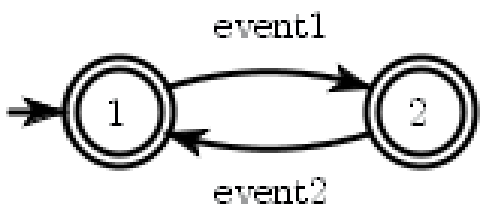
event / $n := \min(n + 1, k)$



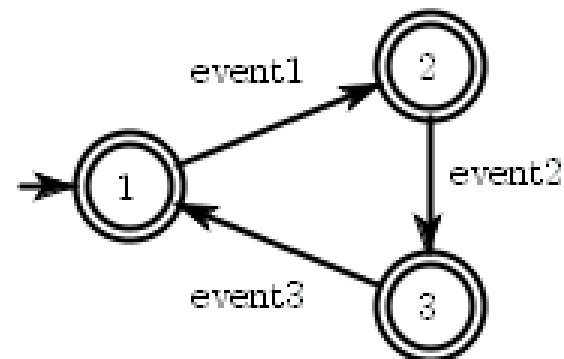


How to parametrize events?

- Sometimes it is necessary to parametrize the *events* of a model rather than the event occurrences.
- Example: k events have to occur in sequence.
 - Cannot be done with variables

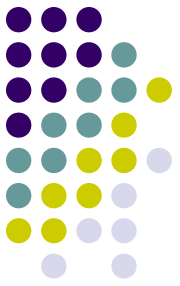


$k=2$



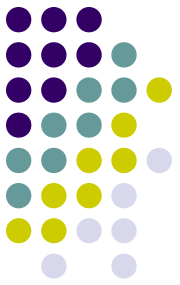
$k=3$

Compositional parametrization

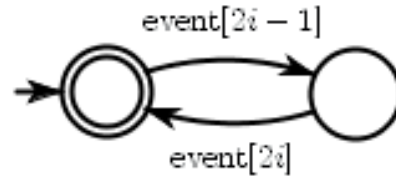


- Define a prototype model with indexed events
 - Indices are functions of i
- Choose a parameter k and get individual components
 - For each i from $lo(k)$ to $hi(k)$, create models where events are indexed accordingly
- Compose the components using synchronous product

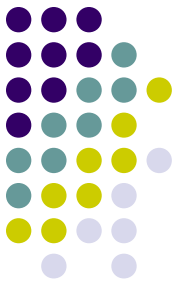
Illustration



Prototype

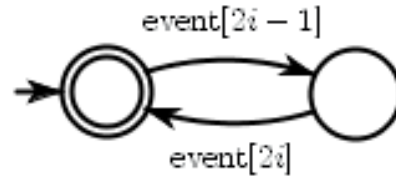


$$\begin{aligned} \text{lo}(k) &= 1 \\ \text{hi}(k) &= k \end{aligned}$$



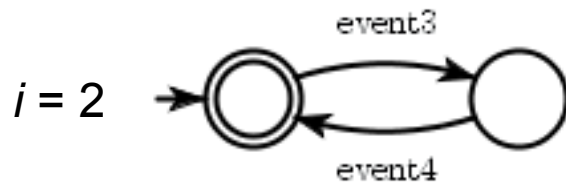
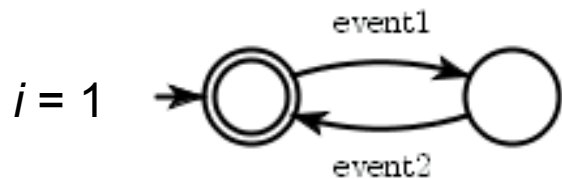
Illustration

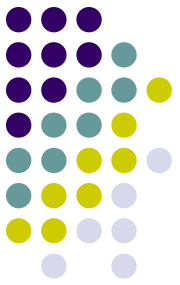
Prototype



$$\text{lo}(k) = 1$$
$$\text{hi}(k) = k$$

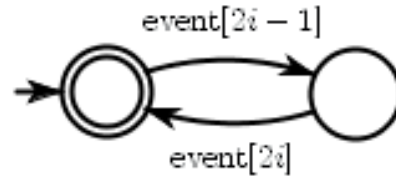
Components for $k = 2$





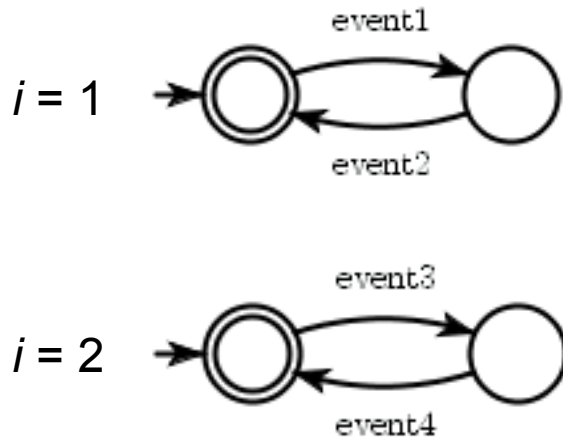
Illustration

Prototype

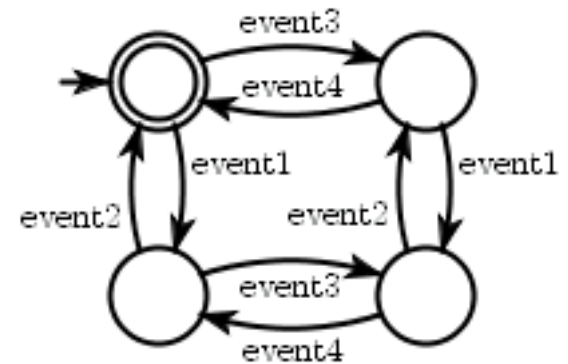


$lo(k) = 1$
 $hi(k) = k$

Components for $k = 2$



Final model for $k = 2$



Compositional parametrization (definition)

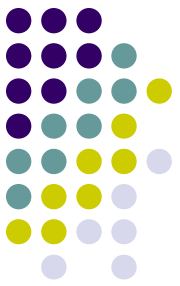


- Let $G^p = (\Sigma_F, Q, \delta, q_0, Q_m)$
 - $\Sigma_F = \{ \sigma_f \mid f \text{ is some function } \mathbf{N} \text{ to } \mathbf{N} \}$
- Let $G^p(i) = (\Sigma(i), Q, \delta(i), q_0, Q_m)$
 - Where σ_f have been replaced by $\sigma_{f(i)}$
- Let $\langle G^p, lo, hi \rangle = \prod_{i \in [lo, hi]} G^p(i)$
- Compositional parametrization

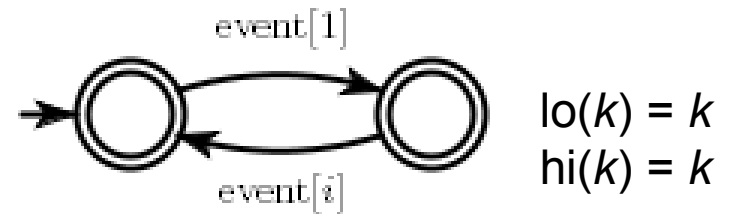
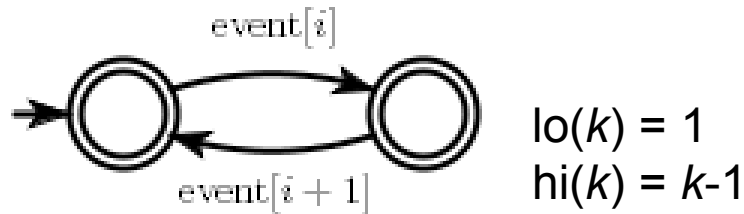
$$G[k] = A \|\langle G^p_{1}, lo_{1}(k), hi_{1}(k) \rangle\| \dots \|\langle G^p_{n}, lo_{n}(k), hi_{n}(k) \rangle\|$$

Example 3

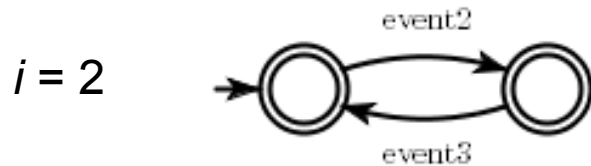
k events occur in sequence



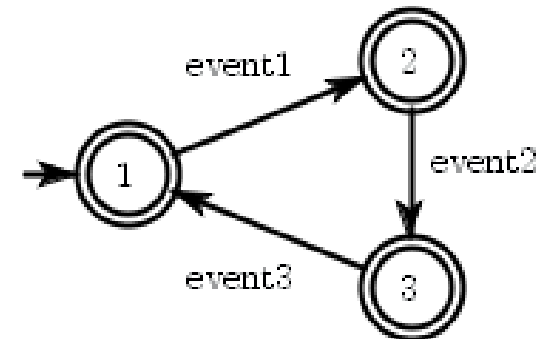
Prototypes



Components for $k = 3$



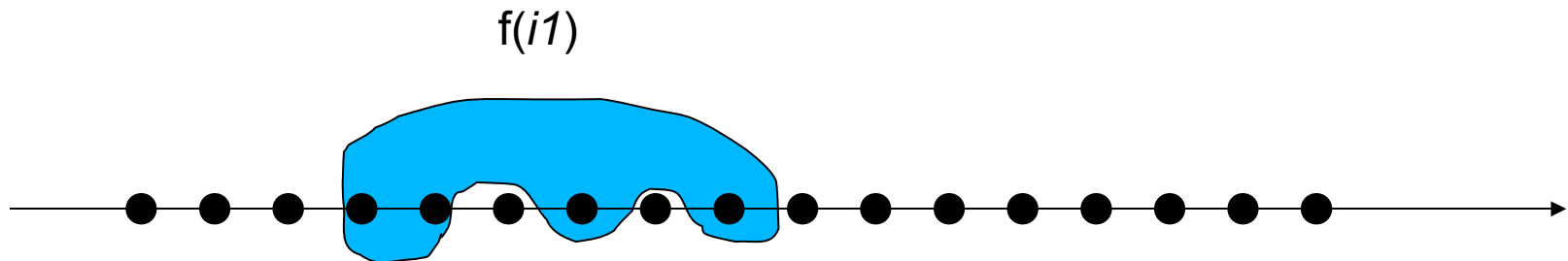
Final model for $k = 3$



Synchronization scope (local)



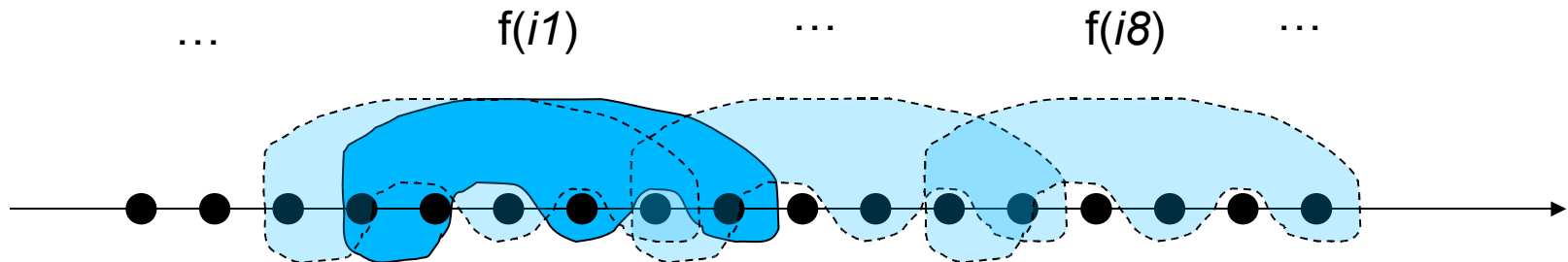
- Event indices can be expressed as a function of i in some range
 - Create repeated patterns of synchronization



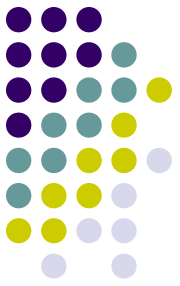
Synchronization scope (local)



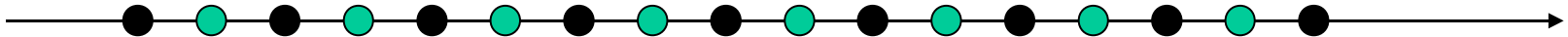
- Event indices can be expressed as a function of i in some range
 - Create repeated patterns of synchronization



Synchronization scope (global)



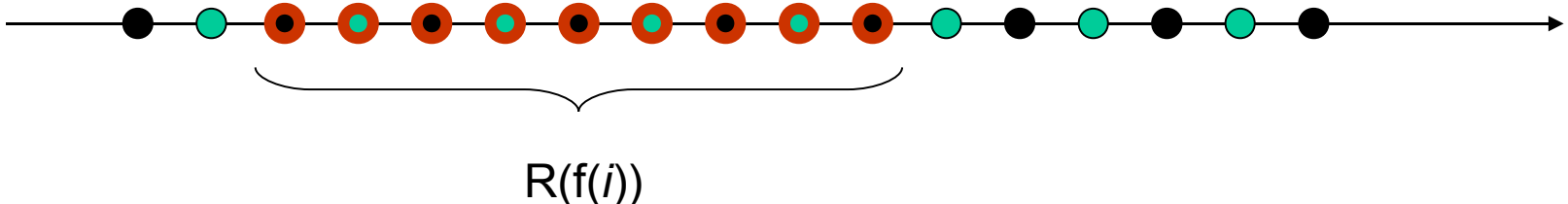
- Sometimes we need to synchronize over *all* events
 - Mutual exclusion
 - **Depends on the specific value of k !**
- Selector transitions
 - Event indices are characteristic functions $h(i)$



Synchronization scope (global)



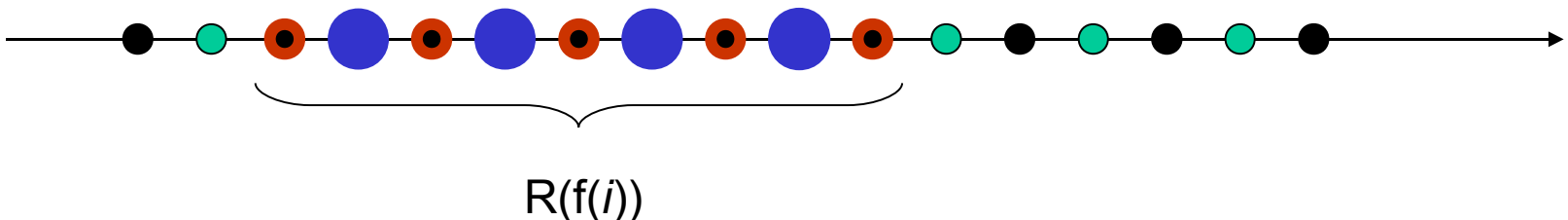
- Sometimes we need to synchronize over *all* events
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Synchronization scope (global)



- Sometimes we need to synchronize over *all* events
 - Mutual exclusion
 - **Depends on the specific value of k !**
- Selector transitions
 - Event indices are characteristic functions $h(i)$



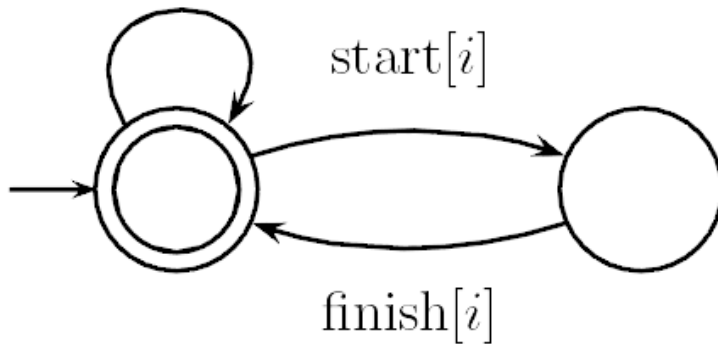
Example 4

Mutual exclusion



Prototype

$$\neg \text{start}[i] \wedge \neg \text{finish}[i]$$

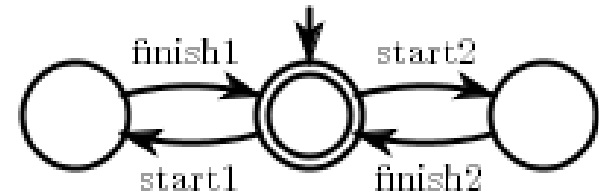


$$\text{lo}(k) = 1$$

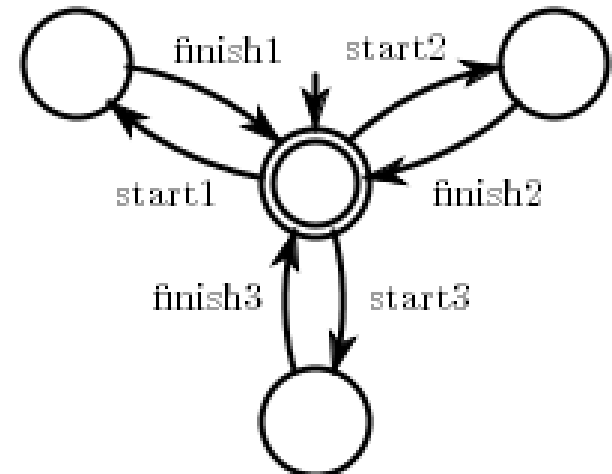
$$\text{hi}(k) = k$$

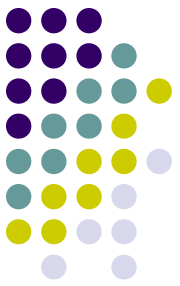
Final models

$k=2$



$k=3$





Final remarks

- We proposed two techniques for the parametrization of templates
- Three types of patterns can be expressed
 - Occurrences of events
 - Local synchronization
 - Non-local synchronization
- Future work
 - Implementation
 - “In-use” parametrization
 - Direct controller synthesis for parametrized models similar to Bherer *et al.* (2009)